

In other words, setting

$$\begin{aligned} R_1^2 &= (x-x')^2 + (y-y')^2 + (z-z')^2, \\ R_2^2 &= (x-x')^2 + (y-y')^2 + (z+z')^2, \\ S_1^2 &= (x-x')^2 + (y-y')^2 \sin^2 \varphi + (z-z')^2 \cos^2 \varphi, \\ S_2^2 &= (x-x')^2 + (y-y')^2 \sin^2 \varphi + (z+z')^2 \cos^2 \varphi, \end{aligned}$$

we find that

$$Q = -\frac{1}{4\pi} \int_{-\infty}^{\infty} \int_0^{\infty} \Delta Q \left(\frac{J_0\left(\frac{2\omega t S_1}{R_1}\right)}{R_1} + \frac{J_0\left(\frac{2\omega t S_2}{R_2}\right)}{R_2} \right) dz' dx' dy' + \dots \quad (12)$$

The obtained integral-differential equation, as in (1), can be solved numerically.

In the solution of (11) the Laplacian of Q_t^0 enters into the right side. Direct practical use of this value presents considerable difficulties. As an approximate value of this magnitude we can use the value of Q_t obtained by interpolation when $t = 0$, allowing that with small t 's we can consider $Q(t) = a_0 + a_1 t + a_2 (t^2/2)$, where the coefficients of a_1 are found from the following conditions:

$$\begin{aligned} \text{when } t = 0 & \quad Q = \bar{Q}^0, \\ \text{when } t = -\delta t & \quad Q = \bar{Q}^{-1}, \\ \text{when } t = -2\delta t & \quad Q = \bar{Q}^{-2}, \end{aligned}$$

whence

$$a_0 = \bar{Q}^0; \quad a_1 = \frac{4(\bar{Q}^0 - \bar{Q}^{-1}) + \bar{Q}^{-2}}{2\delta t}; \quad a_2 = \frac{\bar{Q}^0 - 2\bar{Q}^{-1} + \bar{Q}^{-2}}{\delta t^2}.$$

Thus,

$$\bar{Q}_t^0 = \frac{4(\bar{Q}^0 - \bar{Q}^{-1}) + \bar{Q}^{-2}}{2\delta t},$$

i.e., Q_t^0 is determined from Q values at moments $T \neq 0, -\delta t, -2\delta t$.

THE RECURRENT SYSTEM FOR SOLVING THE PROBLEM OF FORECASTING WITH CONSIDERATION OF INTERNAL FRICTION

Let us examine the system of equations

$$\begin{aligned} \frac{du}{dt} + 2\omega \cos \varphi u - 2\omega \sin \varphi v - \nu \Delta u + \frac{1}{\rho} \frac{\partial p}{\partial x} + \frac{\partial \Phi}{\partial x} &= 0, \\ \frac{dv}{dt} + 2\omega \sin \varphi u - \nu \Delta v + \frac{1}{\rho} \frac{\partial p}{\partial y} + \frac{\partial \Phi}{\partial y} &= 0, \\ \frac{dw}{dt} - 2\omega \cos \varphi w - \nu \Delta w + \frac{1}{\rho} \frac{\partial p}{\partial z} + \frac{\partial \Phi}{\partial z} &= 0, \\ \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} &= 0. \end{aligned} \quad (13)$$

Substitution of variables according to the formulas